

Függvények deriválása

1. Határozd meg az alábbi függvények (x szerinti) deriváltját!

a) $-2x^3 - x^2 + 6x + 2$

$$\boxed{9 + x_2 - 6x_2}$$

b) $-3x^3 - 4x^2 + 5x + 8$

$$\boxed{5 + x_8 - 6x_2}$$

c) $-4x^2 - x - 9$

$$\boxed{-8x - 1}$$

d) $3x^4 - 3x^3 + 4x^2 - 4x - 5$

$$\boxed{12x_3 - 9x_2 + x_8 - 4}$$

e) $8x^3 + 10x^2 + 3x - 6$

$$\boxed{24x_2 + 20x + 3}$$

f) $-10x^2 - 4x + 8$

$$\boxed{-20x - 4}$$

g) $-7x^2 + 8x + 9$

$$\boxed{-14x + 8}$$

h) $x^4 + 5x^3 - 10x^2 - x + 2$

$$\boxed{4x_3 + 15x_2 - 20x - 1}$$

i) $-x^3 + 4x^2 + 3x - 10$

$$\boxed{3 + x_8 + x_2 - 3}$$

j) $-3x + 6$

$$\boxed{3 -}$$

k) $7x + 6$

$$\boxed{7}$$

l) $5x^3 + 4x^2 - 9x - 7$

$$\boxed{6 - x_8 + x_2}$$

m) $4x^3 - 10x^2 - 8x - 1$

$$\boxed{12x_2 - 20x - 8}$$

n) $-4x^2 + 6x + 5$

$$\boxed{9 + x_8 -}$$

o) $-x^3 - 6x^2 + 9x + 3$

$$\boxed{-3x_2 - 12x + 9}$$

p) $-4x^3 + 9x^2 + 8x - 8$

$$\boxed{-12x_2 + 18x + 8}$$

q) $-x^2 + 10x + 5$

$$\boxed{-2x + 10}$$

r) $3x - 1$

$$\boxed{3}$$

s) $-9x^2 - 7x - 8$

$$\boxed{-18x - 7}$$

t) $7x^3 + 6x^2 - 8x - 2$

$$\boxed{21x_2 + 12x - 8}$$

u) $6x^4 - 2x^3 + 5x^2 + 7x - 5$

$$\boxed{24x_3 - 6x_2 + 10x + 7}$$

v) $-2x^2 - 3x - 7$

$$\boxed{-4x - 3}$$

w) $4x^3 + 9x^2 + 2x - 10$

$$\boxed{12x_2 + 18x + 2}$$

x) $3x^3 - 5x^2 - 3x + 9$

$$\boxed{9x_2 - 10x - 3}$$

2. Határozd meg az alábbi függvények (x szerinti) deriváltját!

a) $-2\sqrt[3]{x} - \sqrt[4]{x} + 6\sqrt{x} + \frac{2}{x^3}$

$$\boxed{\frac{4x}{9} - \frac{x\sqrt{x}}{3} + \frac{4\sqrt{x}\sqrt[4]{x}}{1} - \frac{3\sqrt[3]{x}\sqrt[4]{x}}{2}}$$

b) $\frac{5}{x^4} - \sqrt[4]{x} - \frac{4}{x} + 9\sqrt{x}$

$$\boxed{-\frac{x_5}{20} - \frac{4\sqrt[4]{x}}{4} + \frac{x_2}{9} + \frac{2\sqrt{x}}{x}}$$

c) $-\frac{5}{x} - \frac{4}{x^4} + \frac{8}{x^5} + 3\sqrt[4]{x}$

$$\boxed{\frac{ex\sqrt[4]{x}}{3} + \frac{9x}{16} - \frac{40}{x^5} - \frac{5x}{x^4} + \frac{2x}{x^5}}$$

d) $-\frac{7}{x^5} + \frac{8}{x^4} + \frac{9}{x^2}$

$$\boxed{\frac{ex}{35} - \frac{5x}{18} - \frac{9x}{x^5} + \frac{9x}{x^4} + \frac{9x}{x^2}}$$

e) $-\sqrt[5]{x} + \frac{4}{x^5} + \frac{3}{x} - \frac{10}{x^4}$

$$\boxed{-\frac{5\sqrt[5]{x}}{1} - \frac{3}{20} - \frac{x_6}{x^6} - \frac{x_2}{x^2} + \frac{x_5}{40}}$$

f) $7\sqrt[3]{x} + 6\sqrt[5]{x}$

$$\boxed{\frac{7}{3}x\sqrt[3]{x} + \frac{5\sqrt[5]{x}}{9}}$$

g) $\frac{4}{x^3} - 9\sqrt{x} - \frac{7}{x^5}$

$$-\frac{x^{\frac{1}{4}}}{12} - \frac{\sqrt{x}}{9} + \frac{x^{\frac{1}{6}}}{35}$$

h) $-\frac{1}{x} + \frac{10}{x^3} - 4\sqrt[5]{x} + 6\sqrt[3]{x}$

$$+\frac{\sqrt[3]{x^{\frac{1}{4}}}}{2} + \frac{\sqrt[5]{x^{\frac{1}{4}}}}{4} - \frac{\sqrt[5]{x^{\frac{1}{6}}}}{30} + \frac{\sqrt[3]{x^{\frac{1}{2}}}}{1}$$

i) $\frac{5}{x^3} - 4\sqrt{x}$

$$-\frac{x^{\frac{1}{4}}}{15} - \frac{\sqrt{x}}{2}$$

j) $8\sqrt{x} - \frac{8}{x^4}$

$$+\frac{\sqrt{x}}{4} + \frac{\sqrt[4]{x}}{32}$$

k) $\frac{5}{x^4} + \frac{3}{x^5} - \frac{1}{x^3}$

$$-\frac{x^{\frac{1}{5}}}{20} - \frac{x^{\frac{1}{6}}}{15} + \frac{x^{\frac{1}{3}}}{3}$$

l) $\frac{10}{x^2} - 8\sqrt{x} + \frac{7}{x^5} + \frac{6}{x^3}$

$$-\frac{x^{\frac{1}{3}}}{20} - \frac{\sqrt{x}}{4} - \frac{x^{\frac{1}{6}}}{35} - \frac{x^{\frac{1}{4}}}{18}$$

m) $-\frac{2}{x^5} + 6\sqrt{x} + \frac{9}{x^4} + 10\sqrt[5]{x}$

$$+\frac{\sqrt[5]{x^{\frac{1}{4}}}}{2} + \frac{\sqrt[5]{x^{\frac{1}{6}}}}{3} - \frac{\sqrt{x}}{10} + \frac{\sqrt[6]{x}}{36}$$

n) $-\frac{7}{x^3} - 8\sqrt[5]{x} + \frac{4}{x^2}$

$$+\frac{x^{\frac{1}{4}}}{21} - \frac{\sqrt[5]{x^{\frac{1}{4}}}}{8} - \frac{x^{\frac{1}{3}}}{8}$$

o) $-10\sqrt[4]{x} + 3\sqrt{x} - \frac{5}{x^2}$

$$-\frac{\sqrt[4]{x}}{5} + \frac{\sqrt{x}}{3} + \frac{\sqrt[3]{x^{\frac{1}{2}}}}{10}$$

p) $-7\sqrt[3]{x} + \frac{8}{x^5}$

$$-\frac{\sqrt[3]{x^{\frac{1}{2}}}}{7} - \frac{x^{\frac{1}{6}}}{40}$$

q) $-10\sqrt[4]{x} - \frac{7}{x} + 4\sqrt{x} + 5\sqrt[5]{x}$

$$-\frac{\sqrt[4]{x^{\frac{1}{5}}}}{5} + \frac{\sqrt{x}}{2} + \frac{\sqrt[2]{x}}{7} + \frac{\sqrt[5]{x^{\frac{1}{2}}}}{1}$$

r) $-9\sqrt[3]{x} + 7\sqrt[4]{x} + \frac{9}{x^2} + 2\sqrt{x}$

$$\frac{x^{\frac{1}{2}}}{18} + \frac{\sqrt{x}}{7} - \frac{\sqrt[3]{x^{\frac{1}{4}}}}{1} + \frac{\sqrt[4]{x^{\frac{1}{2}}}}{3}$$

s) $-5\sqrt[4]{x} - 8\sqrt{x} + \frac{4}{x}$

$$-\frac{\sqrt[4]{x}}{5} - \frac{\sqrt{x}}{4} - \frac{\sqrt[3]{x}}{4}$$

t) $\frac{8}{x^5} + 5\sqrt[3]{x}$

$$-\frac{x^{\frac{1}{6}}}{40} + \frac{\sqrt[3]{x^{\frac{1}{2}}}}{5}$$

u) $-\frac{6}{x} - 5\sqrt{x} + \frac{3}{x^3}$

$$-\frac{x}{6} - \frac{\sqrt[2]{x}}{5} - \frac{\sqrt[2]{x}}{6} + \frac{x^{\frac{1}{2}}}{9}$$

v) $9\sqrt[4]{x} + 2\sqrt{x} - \frac{3}{x}$

$$\frac{\sqrt[4]{x}}{9} + \frac{\sqrt{x}}{3} - \frac{\sqrt[3]{x^{\frac{1}{2}}}}{1}$$

w) $-9\sqrt{x} - 2\sqrt[5]{x} + \frac{3}{x}$

$$-\frac{\sqrt{x}}{9} - \frac{\sqrt[5]{x}}{2} - \frac{\sqrt[5]{x}}{9}$$

x) $\frac{9}{x^5} - 3\sqrt[4]{x} - 7\sqrt[3]{x} + \frac{7}{x^3}$

$$-\frac{x^{\frac{1}{6}}}{45} - \frac{\sqrt[4]{x}}{3} - \frac{\sqrt[3]{x^{\frac{1}{2}}}}{7} - \frac{x^{\frac{1}{4}}}{21}$$

3. Határozd meg az alábbi szorzatfüggvények (x szerinti) deriváltját!

a) $(-x^3 + 6x^2 + 2x - 3) \cdot (-4x + 9)$

$$16x^3 - 99x^2 + 92x + 30$$

b) $(-x^3 - 4x^2 + 10x - 9) \cdot (3x - 3)$

$$-12x^3 - 27x^2 + 84x - 57$$

c) $(-5x^2 - 4x + 8) \cdot (8x + 3)$

$$-120x^2 - 94x + 52$$

d) $(-10x^2 - 4x + 8) \cdot (-7x + 8)$

$$210x^2 - 104x - 88$$

e) $(8x^3 + x^2 + 5x - 10) \cdot (-x^2 + 10x + 4)$

$$-40x^4 + 316x^3 + 111x^2 + 128x - 80$$

f) $(-2x - 3) \cdot (6x + 7)$

$$-24x - 32$$

g) $(4x^3 - 9x^2 - 7x - 8) \cdot (4x - 10)$

$$64x^3 - 228x^2 + 124x + 38$$

h) $(-x^3 - 4x^2 + 6x + 5) \cdot (-x^2 - 6x + 9)$

$$5x^4 + 40x^3 + 27x^2 - 154x + 24$$

i) $(-4x + 9) \cdot (8x - 8)$

$$-64x + 104$$

j) $(-x^2 + 5x + 3) \cdot (-x^2 + 4x - 9)$

$$4x^3 - 27x^2 + 52x - 33$$

k) $(-7x - 8) \cdot (7x + 6)$

$$86 - x86 -$$

l) $(-8x^2 - 2x + 6) \cdot (6x^2 - 2x + 5)$

$$-192x^3 + 12x^2 - 22$$

m) $(-x - 2) \cdot (-3x^2 - 7x - 8)$

$$9x^2 + 26x + 22$$

n) $(9x^3 + 10x^2 + 2x - 10) \cdot (3x^2 - 5x - 3)$

$$\begin{aligned} & 44 \\ & 213x^2 - 140x + \\ & 135x^4 - 60x^3 - \end{aligned}$$

o) $(-7x^2 + 8x + 3) \cdot (7x^2 + x - 10)$

$$\begin{aligned} & 77 \\ & 147x^2 + 198x - \\ & -196x^3 + \end{aligned}$$

p) $(4x^2 + 5x + 3) \cdot (-5x - 4)$

$$-60x^2 - 82x - 35$$

q) $(7x^2 + 10x + 2) \cdot (-4x^2 - 3x + 4)$

$$\begin{aligned} & 183x^2 - 20x + 34 \\ & -112x^3 - \end{aligned}$$

r) $(-8x^2 + 4x + 2) \cdot (-x + 10)$

$$24x^2 - 168x + 38$$

s) $(-5x^3 - 6x^2 - 2x + 5) \cdot (6x^2 + 7x + 4)$

$$\begin{aligned} & 16x + 27 \\ & 284x^3 - 222x^2 - \\ & -150x^4 - \end{aligned}$$

t) $(3x - 8) \cdot (4x^2 + 9x + 2)$

$$36x^2 - 10x - 96$$

u) $(-5x^3 - 9x^2 - 2x + 3) \cdot (9x^2 - 3x - 7)$

$$\begin{aligned} & 192x + 5 \\ & 264x^3 + 132x^2 + \\ & -225x^4 - \end{aligned}$$

v) $(3x^3 + 7x^2 - 4x + 4) \cdot (-x - 5)$

$$\begin{aligned} & 62x + 16 \\ & -12x^3 - 66x^2 - \end{aligned}$$

w) $(-10x^3 + 3x^2 - 3x + 4) \cdot (-9x^2 - x - 5)$

$$\begin{aligned} & 222x^2 - 96x + 11 \\ & 450x^4 - 68x^3 + \end{aligned}$$

x) $(-5x^3 + 5x^2 + 4x + 2) \cdot (-7x + 6)$

$$\begin{aligned} & 4x + 10 \\ & 140x^3 - 195x^2 + \end{aligned}$$

4. Határozd meg az alábbi hánnyadosfüggvények (x szerinti) deriváltját!

a) $\frac{6x - 1}{-3x + 2}$

$$\frac{(-3x + 2)^2}{6}$$

b) $\frac{10x^2 + 5x + 9}{-4x - 1}$

$$\frac{(-4x - 1)^2}{-40x^2 - 20x + 31}$$

c) $\frac{4x^2 - 3x + 3}{10x^2 - 5x - 4}$

$$\frac{(10x^2 - 5x - 4)^2}{10x^2 - 92x + 27}$$

d) $\frac{10x + 8}{-10x^2 - 6x + 3}$

$$\frac{(-10x^2 - 6x + 3)^2}{100x^2 + 160x + 78}$$

e) $\frac{-7x + 8}{10x^2 + 9x + 8}$

$$\frac{(10x^2 + 9x + 8)^2}{70x^2 - 160x - 128}$$

f) $\frac{-x^2 - 10x + 5}{4x - 1}$

$$\frac{(-4x - 1)^2}{-4x^2 + 2x - 10}$$

g) $\frac{-3x - 2}{7x + 6}$

$$\frac{(7x + 6)^2}{-4}$$

h) $\frac{-9x^2 + 4x + 5}{-8x - 7}$

$$\frac{(-8x - 7)^2}{72x^2 + 126x + 12}$$

i) $\frac{9x^2 - x - 8}{6x - 4}$

$$\frac{(6x - 4)^2}{54x^2 - 72x + 52}$$

j) $\frac{-6x - 1}{-6x + 9}$

$$\frac{(-6x + 9 + x)^2}{72x^2 + 126x + 12}$$

k) $\frac{9x - 4}{-8x + 8}$

$$\frac{40}{(8 + x8 -)^2}$$

l) $\frac{3x^2 + 5x - 1}{-9x^2 + 4x - 1}$

$$\frac{(-9x^2 + 4x - 1)^2}{57x^2 - 24x - 1}$$

m) $\frac{-8x - 7}{6x + 7}$

$$\frac{(-14)(6x + 7)^2}{-14}$$

n) $\frac{6x^2 - 2x - 8}{5x^2 - 2x + 6}$

$$\frac{(-2x^2 + 2x + 6)^2}{5x^2 - 2x - 28}$$

o) $\frac{-2x - 1}{-8x^2 - 7x - 3}$

$$\frac{(-8x^2 - 7x - 3)^2}{-16x^2 - 16x - 1}$$

p) $\frac{10x + 9}{3x^2 - 10x + 2}$

$$\frac{(-30x^2 - 54x + 110)^2}{(3x^2 - 10x + 2)^2}$$

q) $\frac{-7x^2 + 2x - 5}{7x^2 + 3x + 8}$

$$\frac{(7x^2 + 3x + 8)(2x - 1)}{-(35x^2 - 42x + 31)}$$

r) $\frac{-7x - 10}{5x + 4}$

$$\frac{(5x + 4)^2}{22}$$

s) $\frac{-4x^2 - 5x + 3}{9x^2 + 7x - 9}$

$$\frac{(9x^2 + 7x - 9)(2x + 3)}{17x^2 + 18x + 24}$$

t) $\frac{4x^2 - 3x - 4}{-8x - 5}$

$$\frac{(-8x - 5)^2}{-32x^2 - 40x - 17}$$

u) $\frac{2x + 4}{-3x^2 + 10x - 1}$

$$\frac{(6x^2 + 24x - 42)(7x^2 + 10x - 1)}{-(3x^2 + 10x - 1)^2}$$

v) $\frac{5x^2 + 8x - 2}{7x + 6}$

$$\frac{(7x + 9)^2}{35x^2 + 60x + 62}$$

w) $\frac{-5x - 6}{4x^2 - 8x + 3}$

$$\frac{(4x^2 - 8x + 3)(20x^2 + 48x - 63)}{6x^2 + 24x - 42}$$

x) $\frac{10x - 3}{-2x^2 - 9x - 5}$

$$\frac{(-2x^2 - 9x - 5)^2}{20x^2 - 12x - 77}$$

5. Határozd meg az alábbi összetett függvények (x szerinti) deriváltját!

a) $(x^2 - 2x - 1)^8$

$$(2x - 1)^7 \cdot (2x - 1)^8$$

b) $(-3x^2 - 4x + 5)^6$

$$6 \cdot (-3x^2 - 4x + 5)^5 \cdot (-4x - 9)$$

c) $(-4x^2 - x - 9)^9$

$$(1 - 8x)^8 \cdot (-x - 6)$$

d) $(-3x^2 + 4x - 4)^{10}$

$$10 \cdot (-3x^2 + 4x - 4)^9 \cdot (-6x + 4)$$

e) $(-4x^2 + 8x + 9)^9$

$$(8 + x)^8 \cdot (6 + x)^9 \cdot (x - 4)^6$$

f) $(-6x^2 - 10x - 4)^6$

$$6 \cdot (-6x^2 - 10x - 4)^5 \cdot (-12x - 1)$$

g) $(8x^2 - 7x + 10)^7$

$$(7x - 1)^6 \cdot (16x - 7)$$

h) $(8x^2 + x + 5)^5$

$$5 \cdot (x + 1)^4 \cdot (16x + 1)$$

i) $(-x^2 + 10x + 4)^9$

$$9 \cdot (-x^2 + 10x + 4)^8 \cdot (-2x + 10)$$

j) $(-10x^2 - 2x - 3)^9$

$$9 \cdot (-10x^2 - 2x - 3)^8 \cdot (-20x - 2)$$

k) $(7x^2 + 6x + 5)^{10}$

$$10 \cdot (7x^2 + 6x + 5)^9 \cdot (14x + 6)$$

l) $(4x^2 - 9x - 7)^7$

$$7 \cdot (4x^2 - 9x - 7)^6 \cdot (6 - x)$$

m) $(4x^2 - 10x - 8)^6$

$$9 \cdot (4x^2 - 10x - 8)^5 \cdot (8x - 10)$$

n) $(-x^2 - 4x + 6)^6$

$$6 \cdot (-x^2 - 4x - 4)^5 \cdot (9 + x)$$

o) $(-6x^2 + 9x + 10)^9$

$$9 \cdot (-6x^2 + 9x + 10)^8 \cdot (-12x + 9)$$

p) $(5x^2 - 4x + 8)^7$

$$7 \cdot (5x^2 - 4x + 8)^6 \cdot (10x - 4)$$

q) $(-x^2 + 10x + 5)^9$

$$9 \cdot (-x^2 + 10x + 5)^8 \cdot (-2x + 10)$$

r) $(3x^2 - x + 4)^8$

$$8 \cdot (3x^2 - x + 4)^7 \cdot (49 - x)$$

s) $(-9x^2 - 7x - 8)^5$

$$(8 - x)^4 \cdot (x - 1)^5 \cdot (6 - x)$$

t) $(6x^2 - 8x - 2)^5$

$$5 \cdot (6x^2 - 8x - 2)^4 \cdot (12x - 8)$$

u) $(5x^2 + 7x - 1)^5$

$$(1 - x)^4 \cdot (x - 1)^5 \cdot (10x + 5)$$

v) $(-3x^2 - 7x - 8)^7$

$$7 \cdot (-3x^2 - 7x - 8)^6 \cdot (9 - x)$$

w) $(4x^2 + 9x + 2)^{10}$

$$(6 + x)^9 \cdot (4x^2 + 9x + 2)^9$$

x) $(-10x^2 + 3x - 5)^{10}$

$$10 \cdot (-10x^2 + 3x - 5)^9 \cdot (-20x + 3)$$

6. Határozd meg az alábbi összetett függvények (x szerinti) deriváltját!

a) $10^{\cos x}$

$$-10^{\cos x} \cdot \sin x \cdot \ln 10$$

b) $\sqrt[9]{-3x^2 - 4x + 5}$

$$\frac{9\sqrt[9]{(-3x^2 - 4x + 5)^8}}{-6x - 4}$$

c) $8^{-x^2 - 9x + 3}$

$$(8^{-x^2 - 9x + 3})' = 8^{-x^2 - 9x + 3} \cdot \ln 8 \cdot (-2x - 9)$$

d) $19^{\sin x}$

$$(19^{\sin x})' = 19^{\sin x} \cdot \cos x \cdot \ln 19$$

e) $\log_7(8x^2 + 3x - 6)$

$$(\log_7(8x^2 + 3x - 6))' = \frac{\ln 7 \cdot (8x^2 + 3x - 6)}{16x + 3}$$

f) $2^{-4x^2 + 8x - 7}$

$$(2^{-4x^2 + 8x - 7})' = 2^{-4x^2 + 8x - 7} \cdot \ln 2 \cdot (-8x + 8)$$

g) $\log_4(9x^2 + 8x + 1)$

$$(\log_4(9x^2 + 8x + 1))' = \frac{\ln 4 \cdot (9x^2 + 8x + 1)}{18x + 8}$$

h) $\cos(-x^2 + 4x + 3)$

$$(\cos(-x^2 + 4x + 3))' = -\sin(-x^2 + 4x + 3) \cdot (-2x + 4)$$

i) $\sin(-3x^2 + 6x + 7)$

$$(\sin(-3x^2 + 6x + 7))' = (\cos(-3x^2 + 6x + 7)) \cdot (-6x + 6)$$

j) $5^{-8x^2 + 4x - 10}$

$$(5^{-8x^2 + 4x - 10})' = 5^{-8x^2 + 4x - 10} \cdot \ln 5 \cdot (-16x + 4)$$

k) $11^{\cos x}$

$$(11^{\cos x})' = 11^{\cos x} \cdot \sin x \cdot \ln 11$$

l) $8^{6x^2 + 5x - 1}$

$$(8^{6x^2 + 5x - 1})' = 8^{6x^2 + 5x - 1} \cdot \ln 8 \cdot (12x + 5)$$

m) $\log_5(-6x^2 + 3x + 5)$

$$(\log_5(-6x^2 + 3x + 5))' = \frac{\ln 5 \cdot (-6x^2 + 3x + 5)}{-12x + 3}$$

n) $19^{\sin x}$

$$(19^{\sin x})' = 19^{\sin x} \cdot \cos x \cdot \ln 19$$

o) $11^{5x^2 + 3x - 1}$

$$(11^{5x^2 + 3x - 1})' = 11^{5x^2 + 3x - 1} \cdot \ln 11 \cdot (10x + 3)$$

p) $\sqrt[4]{-7x^2 - 8x + 7}$

$$\frac{4\sqrt[4]{(-7x^2 - 8x + 7)^3}}{-14x - 8}$$

q) $\sqrt[8]{-8x^2 - 2x + 6}$

$$(\sqrt[8]{-8x^2 - 2x + 6})' = \frac{8\sqrt[8]{(-8x^2 - 2x + 6)^7}}{-16x - 2}$$

r) $\sin(5x^2 + 7x - 1)$

$$(\sin(5x^2 + 7x - 1))' = \cos(5x^2 + 7x - 1) \cdot (10x + 7)$$

s) $\cos(-7x^2 - 8x + 4)$

$$(\cos(-7x^2 - 8x + 4))' = -\sin(-7x^2 - 8x + 4) \cdot (-14x - 8)$$

t) $20^{\cos x}$

$$(20^{\cos x})' = 20^{\cos x} \cdot \sin x \cdot \ln 20$$

u) $2^{3x^2 - 5x - 3}$

$$(2^{3x^2 - 5x - 3})' = (2^{\ln 2 \cdot (3x^2 - 5x - 3)})' = (\ln 2 \cdot (3x^2 - 5x - 3)) \cdot 2^{3x^2 - 5x - 3} \cdot \ln 2$$

v) $\sqrt[7]{-7x^2 + 8x + 3}$

$$\frac{7\sqrt[7]{(-7x^2 + 8x + 3)^6}}{-14x + 8}$$

w) $\sin(-10x^2 - 7x + 4)$

$$(\sin(-10x^2 - 7x + 4))' = \cos(-10x^2 - 7x + 4) \cdot (-20x - 7)$$

x) $\sqrt[5]{-5x^2 - 4x - 9}$

$$\frac{5\sqrt[5]{(-5x^2 - 4x - 9)^4}}{-10x - 4}$$

y) $\log_3(7x^2 + 2x - 4)$

$$(\log_3(7x^2 + 2x - 4))' = \frac{\ln 3 \cdot (7x^2 + 2x - 4)}{14x + 2}$$

z) $\sqrt[8]{4x^2 - 5x - 8}$

$$\frac{8\sqrt[8]{(4x^2 - 5x - 8)^7}}{-5x - 8}$$

aa) $15^{\cos x}$

$$(15^{\cos x})' = 15^{\cos x} \cdot \sin x \cdot \ln 15$$

ab) $11^{-3x^2 - 5x - 6}$

$$(11^{-3x^2 - 5x - 6})' = 11^{-3x^2 - 5x - 6} \cdot \ln 11 \cdot (-6x - 5)$$

ac) $\sin(8x^2 + 5x + 6)$

$$(\sin(8x^2 + 5x + 6))' = \cos(8x^2 + 5x + 6) \cdot (16x + 5)$$

ad) $\sqrt[3]{4x^2 - 6x - 5}$

$$\frac{3\sqrt[3]{(4x^2 - 6x - 5)^2}}{9 - 8x}$$

ae) $\log_9(-8x^2 + 4x + 2)$

$$(\log_9(-8x^2 + 4x + 2))' = \frac{\ln 9 \cdot (-8x^2 + 4x + 2)}{-18x - 2}$$

af) $\log_6(-9x^2 - 2x + 3)$

$$(\log_6(-9x^2 - 2x + 3))' = \frac{\ln 6 \cdot (-9x^2 - 2x + 3)}{-18x - 2}$$

$$\text{ag} \log_9(9x^2 - 3x - 7)$$

$$\frac{(\underline{\lambda} - x\underline{\varepsilon})^{x_6} \cdot \underline{\lambda}^6}{\underline{\lambda}^{8x-3}}$$

$$\text{ah} \sin(7x^2 - 4x + 4)$$

$$\frac{(\underline{\lambda} 4x - \underline{\lambda})}{\cos(\underline{\lambda} x^2 - \underline{\lambda} x + \underline{\lambda})}.$$

$$\text{ai) } 7^{-4x^2 - 7x - 10}$$

$$(\underline{\lambda} - x\underline{\varepsilon}) \cdot \underline{\lambda} \cdot \underline{\lambda}^{10-x\underline{\varepsilon}} \cdot \underline{\lambda}^{x_4 - \underline{\lambda}}$$

$$\text{aj) } \sqrt[7]{-3x^2 + 4x - 9}$$

$$\frac{\underline{\lambda}^6(-6x^2 + 4x - 1)}{\underline{\lambda}^{6x+4}}$$

$$\text{ak) } 7^{-5x^2 + 5x + 4}$$

$$(\underline{\lambda} + x\underline{\varepsilon}) \cdot \underline{\lambda} \cdot \underline{\lambda}^{10+x\underline{\varepsilon}} \cdot \underline{\lambda}^{x_5 + \underline{\lambda}}$$

$$\text{al) } \sqrt[9]{-7x^2 + 6x + 3}$$

$$\frac{\underline{\lambda}^6(x + 6x^2 - 1)}{\underline{\lambda}^{14x+6}}$$

$$\text{am} \cos(x^2 - 8x - 9)$$

$$\cdot \frac{(8 - x\underline{\varepsilon})}{(6 - x\underline{\varepsilon})^x} - \sin$$

$$\text{an) } \cos(6x^2 - 4x - 10)$$

$$\frac{(\underline{\lambda} 2x - \underline{\lambda})}{-\sin(6x^2 - 4x - 10)}.$$

$$\text{ao) } \sin(-5x^2 + 10x + 4)$$

$$\cos(-5x^2 + 10x + 4) \cdot$$

$$\text{ap) } 15^{-9x^2 + 7x - 7}$$

$$\underline{\lambda}^{5-9x^2+7x-7} \cdot \underline{\lambda} \cdot (-18x + \underline{\lambda})$$

$$\text{aq) } 8^{\sin x}$$

$$8^{\sin x} \cdot \cos x \cdot \underline{\lambda} 8$$

$$\text{ar) } \sqrt[9]{-9x^2 + 5x - 10}$$

$$\frac{\underline{\lambda}^6(-9x^2 + 5x - 10)}{\underline{\lambda}^{18x+5}}$$

$$\text{as) } \log_6(5x^2 - 2x + 8)$$

$$\frac{\underline{\lambda} 6 \cdot (5 - 2x)}{10x - 2}$$

$$\text{at) } \log_6(-2x^2 + 4x - 1)$$

$$\frac{\underline{\lambda} 6 \cdot (-2x^2 + 4x - 1)}{-4x + 4}$$

$$\text{au) } \sqrt[7]{-6x^2 + 6x + 10}$$

$$\underline{\lambda}^7 \cdot \underline{\lambda}^{(-6x^2 + 6x + 10)} \cdot$$

$$\text{av) } 8^{4x^2 + 3x + 1}$$

$$(x + 8) \cdot \underline{\lambda} 8 \cdot \underline{\lambda} 8$$

7. Határozd meg az alábbi függvények x_0 abszcísszájú pontjába húzható érintő egyenletét!

$$\text{a) } -3x^5 - 4x^4 + 2x^3 + 6x^2 - x - 2$$

$$x_0 = 0$$

$$\underline{\lambda} - x - = \underline{\lambda}$$

$$\text{b) } 7x^5 - 4x^4 - x^3 + 10x^2 + 5x + 9$$

$$x_0 = -4$$

$$y = 9861x + 31465$$

$$\text{c) } -5x^3 - 4x^2 + 4x - 3$$

$$x_0 = 1$$

$$\underline{\lambda} 11 - 19x + \underline{\lambda} = \underline{\lambda}$$

$$\text{d) } -10x^5 - x^4 - 6x^3 + 3x^2 + 10x + 8$$

$$x_0 = 1$$

$$09 + 56x - = \underline{\lambda}$$

$$\text{e) } 5x^4 + x^3 + 10x^2 - 7x + 8$$

$$x_0 = -5$$

$$y = -2532x - 9367$$

$$\text{f) } -2x^4 - 10x^3 + 3x^2 + 4x - 1$$

$$x_0 = 3$$

$$866 + -44x = \underline{\lambda}$$

$$\text{g) } 4x^3 + 5x^2 + 6x + 7$$

$$x_0 = 2$$

$$\underline{\lambda} 77 - 4x - \underline{\lambda} = \underline{\lambda}$$

$$\text{h) } 9x^4 - 10x^3 + 4x^2 - 8x - 7$$

$$x_0 = 4$$

$$y = 1848x - 5703$$

$$\text{i) } -6x^4 - x^3 + 5x^2 + 6x - 4$$

$$x_0 = -3$$

$$y = 1355x + 1355$$

$$\text{j) } -4x^3 + 5x^2 + 3x - 6$$

$$x_0 = -3$$

$$y = -135x - 267$$

$$\text{k) } 4x^4 + 10x^3 - x^2 - 8x + 8$$

$$x_0 = 5$$

$$y = 2732x + \underline{\lambda}$$

$$\text{l) } 4x^3 - x^2 + 3x + 5$$

$$x_0 = -4$$

$$y = 203x + 533$$

$$\text{m) } 6x^3 + 7x^2 - 8x - 7$$

$$x_0 = -2$$

$$y = 38x + 61$$

$$\text{n) } 9x^4 + 8x^3 + 6x^2 - 2x - 8$$

$$x_0 = -5$$

$$y = -3962x - 15033$$

o) $-8x^4 - 7x^3 - 3x^2 - 2x - 1$
 $x_0 = 5$

$$y = -4557x + 16824$$

p) $5x^4 - 10x^3 + 2x^2 + 10x + 9$
 $x_0 = 0$

$$y = 10x + 9$$

q) $-4x^4 + 3x^3 + 8x^2 - 7x + 2$
 $x_0 = -5$

$$y = 2138x + 8052$$

r) $-3x^5 + 2x^4 + 5x^3 + 4x^2 - 7x - 10$
 $x_0 = 0$

$$y = -7x - 10$$

s) $7x^3 - 9x^2 - 4x + 10$
 $x_0 = -5$

$$y = 611x + 1985$$

t) $-6x^5 + x^4 - 5x^3 + 4x^2 - 3x - 4$
 $x_0 = -3$

$$y = -2700x - 6385$$

u) $x^5 + 6x^4 + 8x^3 - x^2 + 2x + 4$
 $x_0 = 2$

$$y = 366x - 536$$

v) $6x^4 + 5x^3 + 8x^2 - 2x - 6$
 $x_0 = -5$

$$y = -2707x - 10206$$

w) $9x^5 + 5x^4 + 3x^3 - 5x^2 - 6x + 4$
 $x_0 = 0$

$$y = x9 - 4$$

x) $7x^5 + 5x^4 - 3x^3 + 2x^2 + 9x + 4$
 $x_0 = 0$

$$y = 4x + 6$$