

# Szorzattá alakítások II.

1. Alakítsd a következő kifejezéseket szorzattá!

- |  |  |   |  |
|--|--|---|--|
| a) $121k^{20} - 110b^8k^{10} + 25b^{16}$ | $\boxed{(\frac{1}{2}k^8 - \frac{1}{11}b^4)^2}$                                       | b) $144f^2 + 100 + 240f$                | $\boxed{(\frac{1}{2}f + 10)^2}$  |
| c) $72j^8h^9 + 144h^{18} + 9j^{16}$      | $\boxed{(\frac{3}{2}j^4 + 12h^9)^2}$   | d) $121 + 4j^2 - 44j$                   | $\boxed{(2j - 11)^2}$  |
| e) $16b^{20} - 81f^{18}$                 | $\boxed{(\frac{4}{9}f^9 - \frac{1}{16}b^{10})(\frac{4}{9}f^9 + \frac{1}{16}b^{10})}$ | f) $-198u + 81u^2 + 121$                | $\boxed{(9u - 11)^2}$  |
| g) $9b^4 - 64v^4$                        | $\boxed{(\frac{3}{2}b^2 - 8v^2)(\frac{3}{2}b^2 + 8v^2)}$                             | h) $144x^{14} + 96x^7b^{10} + 16b^{20}$ | $\boxed{(\frac{1}{2}x^7 + 4b^{10})^2}$   |
| i) $4b^{14} + 36x^{10} - 24x^5b^7$       | $\boxed{(\frac{1}{2}bx^5 - 2b^7)^2}$   | j) $121d^{14} - 81f^{12}$               | $\boxed{(\frac{1}{9}f^6 + \frac{1}{11}d^7)(\frac{1}{9}f^6 - \frac{1}{11}d^7)}$ |
| k) $121 + 49x^2 + 154x$                  | $\boxed{(\frac{1}{2}x + 11)^2}$  | l) $4z^8 - 9u^{12}$                     | $\boxed{(\frac{1}{2}z^4 + 3u^6)(\frac{1}{2}z^4 - 3u^6)}$                       |
| m) $9v^8 - 36h^{12}$                     | $\boxed{(\frac{1}{9}vh^4 + \frac{1}{4}v^4)(\frac{1}{9}vh^4 - \frac{1}{4}v^4)}$       | n) $-20d + 25d^2 + 4$                   | $\boxed{(\frac{1}{2}d - 2)^2}$   |
| o) $126f + 49f^2 + 81$                   | $\boxed{(\frac{1}{2}f + 9)^2}$   | p) $72v^5z^8 + 81z^{16} + 16v^{10}$     | $\boxed{(\frac{1}{8}z^6 + v^5)^2}$   |
| q) $-24h^5z^4 + 9h^{10} + 16z^8$         | $\boxed{(\frac{1}{4}hz^4 - \frac{1}{2}h^5)(\frac{1}{4}hz^4 + h^5)}$                  | r) $16h^{20} + 81b^{12} - 72h^{10}b^6$  | $\boxed{(\frac{1}{2}h^{10} - \frac{1}{9}b^6)^2}$                               |
| s) $121k^6 - 36g^{10}$                   | $\boxed{(\frac{1}{11}k^3 - \frac{1}{6}g^5)(\frac{1}{11}k^3 + \frac{1}{6}g^5)}$       | t) $4 + 49e^2 + 28e$                    | $\boxed{(\frac{1}{2}e + 2)^2}$   |
| u) $9e^2 + 16 + 24e$                     | $\boxed{(\frac{1}{2}e + 4)^2}$   | v) $-24b^4d^6 + 36d^{12} + 4b^8$        | $\boxed{(\frac{1}{2}d^6 - \frac{1}{4}b^4)^2}$                                  |
| w) $49a^8 - 36y^{20}$                    | $\boxed{(\frac{1}{7}a^4 + \frac{1}{4}y^{10})(\frac{1}{7}a^4 - \frac{1}{4}y^{10})}$   | x) $64 + 4z^2 + 32z$                    | $\boxed{(\frac{1}{2}z + 8)^2}$   |
| y) $144w^{12} + 64b^6 + 192b^3w^6$       | $\boxed{(\frac{1}{2}w^6 + \frac{1}{4}b^3)^2}$  | z) $-80b + 16b^2 + 100$                 | $\boxed{(\frac{1}{4}b - 10)^2}$  |

2. Alakítsd a következő kifejezéseket szorzattá!

- |                                 |                               |                                  |                                |
|---------------------------------|-------------------------------|----------------------------------|--------------------------------|
| a) $48jb + 18uy - 48jy - 18ub$  | $\boxed{(bj - 9y)(nu - l8)}$  | b) $-96hz + 32uz - 28ux + 84hx$  | $\boxed{(xL - z8)(4u - 12h)}$  |
| c) $-42ez + 35ey + 30xz - 25xy$ | $\boxed{(z9 - h9)(xG - eL)}$  | d) $9vh - 24vb - 16wb + 6wh$     | $\boxed{(q8 - pE)(nZ + oE)}$   |
| e) $-90ga + 30fh + 60fa - 45gh$ | $\boxed{(h6 - f9)(10a + g5)}$ | f) $-18uh + 20ub - 90wh + 100wb$ | $\boxed{(2u + 10w)(10b - 9h)}$ |

g)	$-25jc + 35wc + 49wf - 35jf$	$(f_{12} - f_7)(f_{12} + f_7)$	h)	$60bv - 60bc - 60uc + 60uv$	$(f_{12} + f_6)(f_{12} - f_6)$
i)	$-20gy + 8gd + 24xd - 60xy$	$(f_9 + f_6)(f_4 - f_{10})$	j)	$-16uz + 48uy + 96ky - 32kz$	$(f_{8k} + f_{4u})(f_{12y} - f_{4z})$
k)	$36jf - 48jw + 24cf - 32cw$	$(f_{12} - f_9)(f_4 + f_6)$	l)	$3uj - 33cj - 7ub + 77cb$	$(f_{11c} - f_{1u})(f_{7b} - f_{3j})$
m)	$40aw + 132fh - 60fw - 88ah$	$(f_{12} - f_8)(f_{11h} - f_5w)$	n)	$108df - 144de + 60ze - 45zf$	$(f_{5z} - f_{12d})(f_{12e} - f_9f)$
o)	$40jk + 81xh + 36xk + 90jh$	$(f_9x + f_{10j})(f_{4k} + f_{9h})$	p)	$121ab + 144dh + 132db + 132ah$	$(f_{12d} + f_{11a})(f_{12h} + f_{11b})$
q)	$-60aj + 60ye + 144yj - 25ae$	$(f_{12y} - f_5a)(f_{5e} + f_{12j})$	r)	$-22fv + 110fc - 20wc + 4uv$	$(f_{2u} - f_{11f})(f_{2a} - f_{10c})$
s)	$24dc + 24bc + 24dh + 24bh$	$(f_{3h} + f_{3c})(p_8 + q_8)$	t)	$24xg - 40fu + 40fg - 24xu$	$(f_{6x} + f_{10f})(f_{4g} - f_{4u})$
u)	$8aj + 22wj + 8ag + 22wg$	$(f_{4a} + f_{11w})(f_{2y} + f_{2j})$	v)	$88gb - 56fk - 56fb + 88gk$	$(f_{11g} - f_7f)(f_{8k} + f_{4b})$
w)	$-100fa + 81eg - 90fg + 90ea$	$(f_{9e} - f_{10f})(f_{9g} + f_{10a})$	x)	$42fk + 56fe - 96he - 72hk$	$(f_{7f} - f_{12h})(f_{8e} + f_{6k})$
y)	$2ca - 18cf - 2ua + 18uf$	$(f_{2u} - f_{2c})(f_6 - f_{1a})$	z)	$77zh - 49zg + 132yh - 84yg$	$(f_{7z} + f_{12y})(f_{11h} - f_{7g})$

3. Alakítsd a következő kifejezéseket szorzattá!

a)	$h^{36} - 34h^{18} + 81$	$(f_{18} + f_{4h} - 9)(h_{18} - f_{4h} - 9)$	b)	$f^{36} - 108f^{18} + 16$	$(f_{18} + f_{10f} - 4)(f_{18} - f_{10f} - 4)$
c)	$b^{12} + 2b^6 + 9$	$(f_6 + 2f_3 + 3)(f_6 - 2f_3 + 3)$	d)	$j^{40} - 125j^{20} + 4$	$(f_{20} + f_{11j} - 2)(f_{20} - f_{11j} - 2)$
e)	$u^{16} - 154u^8 + 25$	$(f_8 + 12f_4 - 8)(f_8 - 12f_4 - 5)$	f)	$x^{20} - 29x^{10} + 100$	$(x_{10} + 7x_5 + 10)(x_{10} - 7x_5 + 10)$
g)	$h^{28} - 67h^{14} + 81$	$(f_{14} + 7f_7 - 9)(f_{14} - 7f_7 + 9)$	h)	$j^{20} - 24j^{10} + 16$	$(f_{10} + 4f_5 - 4)(f_{10} - 4f_5 - 4)$
i)	$k^{12} - 56k^6 + 100$	$(f_6 + 6f_3 - 10)(f_6 - 6f_3 - 10)$	j)	$g^{16} - 120g^8 + 144$	$(f_8 + 12f_4 + 12)(f_8 - 12f_4 + 12)$
k)	$f^8 - 107f^4 + 49$	$(f_4 + 11f_2 + 7)(f_4 - 11f_2 + 7)$	l)	$x^{44} - 101x^{22} + 100$	$(x_{22} + 9x_{11} - 10)(x_{22} - 9x_{11} - 10)$
m)	$y^{28} - 137y^{14} + 64$	$(f_{14} + 11f_7 - 8)(f_{14} - 11f_7 - 8)$	n)	$e^{28} - 77e^{14} + 4$	$(e_{14} + 9e_7 + 2)(e_{14} - 9e_7 + 2)$
o)	$d^{16} - 40d^8 + 144$	$(f_8 + 4d_4 - 12)(f_8 - 4d_4 - 12)$	p)	$a^{44} - 126a^{22} + 81$	$(a_{22} + 12a_{11} + 9)(a_{22} - 12a_{11} + 9)$
q)	$d^8 - 114d^4 + 49$	$(f_4 + 10d_2 - 7)(f_4 - 10d_2 - 7)$	r)	$y^{12} - 50y^6 + 49$	$(f_6 + 8 - f_9)(f_6 + 8 + f_9)$